YEAR 10 – SIMILARITY...
Congruence, similarity & enlargement

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:
- Enlarge by a positive scale factor
- Enlarge by a fractional scale factor
- Identify similar shapes
- Work out missing sides and angles in similar shapes
- Use parallel lines to find missing angles
- Understand similarity and congruence

Keywords

Enlarge: to make a shape bigger (or smaller) by a given multiplier (scale factor)
Scale Factor: the multiplier of enlargement
Centre of enlargement: the point the shape is enlarged from
Similar: when one shape can become another with a reflection, rotation, enlargement or translation.
Congruent: the same size and shape
Corresponding: items that appear in the same place in two similar situations
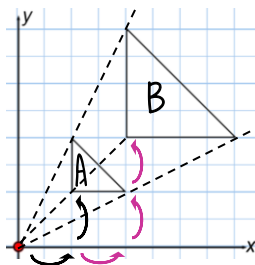**Parallel**: straight lines that never meet (equal gradients)

Positive scale factors 🔴

Enlargement from a point
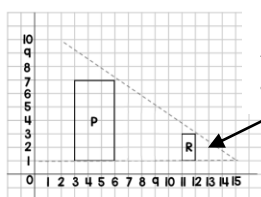Enlarge shape A by SF 2 from (0,0)

The shape is enlarged by 2

The distance from the point enlarges by 2

Fractional scale factors 🔴

Fractions less than 1 make a shape SMALLER

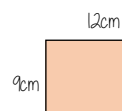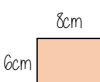R is an enlargement of P by a scale factor $\frac{1}{3}$ from centre of enlargement (15,1)

SF: $\frac{1}{3}$ – R is three times smaller than P

Identify similar shapes

Angles in similar shapes do not change.
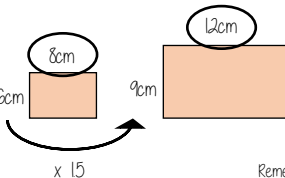e.g. if a triangle gets bigger the angles can not go above $180°$

Similar shapes

8cm
6cm
12cm
9cm

Scale Factor:
Both sides on the bigger shape are 1.5 times bigger

Compare sides: 6 : 9   8 : 12
              2 : 3 **2 : 3**

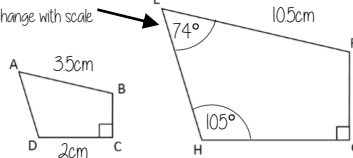Both sets of sides are in the same ratio

Information in similar shapes

8cm
6cm
12cm
9cm

x 1.5

Compare the equivalent side on both shapes

Scale Factor is the multiplicative relationship between the two lengths

Shape ABCD and EFGH are similar

Notation helps us find the corresponding sides

AB and EF are corresponding

Remember angles do not increase or change with scale

E 74° 10.5cm F
A 3.5cm B
D 2cm C
H 105° G

Angles in parallel lines 🔴

Alternate angles

30°
30°
150°
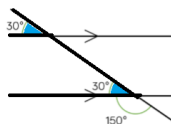
Because alternate angles are equal the highlighted angles are the same size
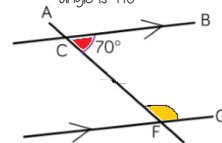
Corresponding angles

55°
55°

Because corresponding angles are equal the highlighted angles are the same size

Co-interior angles

Because co-interior angles have a sum of $180°$ the highlighted angle is $110°$

A B
C 70°
F G

As angles on a line add up to $180°$ co-interior angles can also be calculated from applying alternate/ corresponding rules first

Similar triangles

Shares a vertex

Because corresponding angles are equal the highlighted angles are the same size

Parallel lines – all angles will be the same in both triangle

As all angles are the same this is similar – it only one pair of sides are needed to show equality

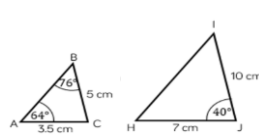All the angles in both triangles are the same and so similar

Vertically opposite angles

Congruence and Similarity

Congruent shapes are identical – all corresponding sides and angles are the same size

B 76° 5 cm
A 64° 3.5 cm C
L
K 40° 5 cm
3.5 cm M

$Q\hat{C}B = K\hat{M}L$
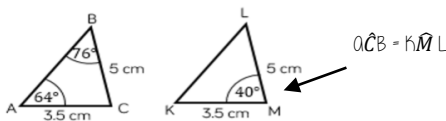
Because all the angles are the same and QC=KM BC=LM triangles QBC and KLM are **congruent**

B 76° 5 cm
A 64° 3.5 cm C
I 10 cm
H 7 cm 40° J

Because all angles are the same, but all sides are enlarged by 2 QBC and HIJ are **similar**

Conditions for congruent triangles

Triangles are congruent if they satisfy any of the following conditions

Side-side-side

All three sides on the triangle are the same size

Angle-side-angle

Two angles and the side connecting them are equal in two triangles

Side-angle-side

Two sides and the angle in-between them are equal in two triangles (it will also mean the third side is the same size on both shapes)

Right angle-hypotenuse-side

The triangles both have a right angle, the hypotenuse and one side are the same