

# Angles in parallel and polygons

@whistomaths

## What do I need to be able to do?

By the end of this unit you should be able to:

- Identify alternate angles
- Identify corresponding angles
- Identify co-interior angles
- Find the sum of interior angles in polygons
- Find the sum of exterior angles in polygons
- Find interior angles in regular polygons

## Keywords

**Parallel:** Straight lines that never meet

**Angle:** The figure formed by two straight lines meeting (measured in degrees)

**Transversal:** A line that cuts across two or more other (normally parallel) lines

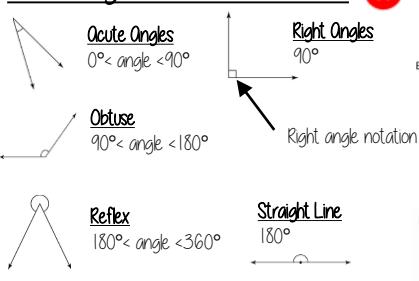
**Isosceles:** Two equal size lines and equal size angles (in a triangle or trapezium)

**Polygon:** A 2D shape made with straight lines

**Sum:** Addition (total of all the interior angles added together)

**Regular polygon:** All the sides have equal length; all the interior angles have equal size.

## Basic angle rules and notation R



The letter in the middle is the angle  
The arc represents the part of the angle

**Angle Notation:** three letters ABC

This is the angle at B =  $113^\circ$

**Line Notation:** two letters EC

The line that joins E to C

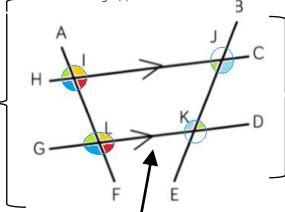
**Vertically opposite angles**

Equal angles around a point

$360^\circ$

## Parallel lines

Still remember to look for angles on straight lines, around a point and vertically opposite!

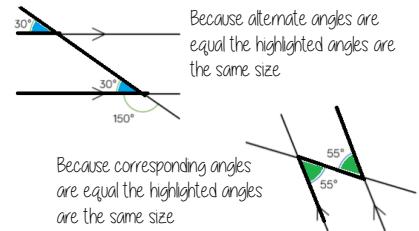


Lines QF and BE are **transversals** (lines that bisect the parallel lines)

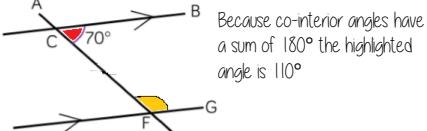
Alternate angles often identified by their "Z shape" in position

This notation identifies parallel lines

## Alternate/ Corresponding angles

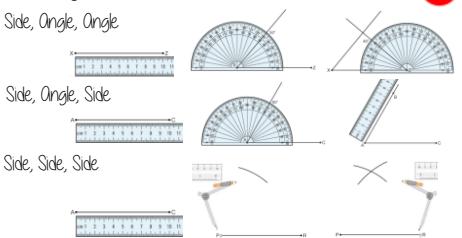


## Co-interior angles



As angles on a line add up to  $180^\circ$  co-interior angles can also be calculated from applying alternate/ corresponding rules first

## Triangles & Quadrilaterals R



## Properties of Quadrilaterals

<b>Square</b>	All sides equal size
	All angles $90^\circ$
	Opposite sides are parallel
<b>Rectangle</b>	All angles $90^\circ$
	Opposite sides are parallel
<b>Rhombus</b>	All sides equal size
	Opposite angles are equal

### Parallelogram

Opposite sides are parallel  
Opposite angles are equal  
Co-interior angles

### Trapezium

One pair of parallel lines

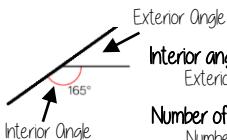
### Kite

No parallel lines  
Equal lengths on top sides  
Equal lengths on bottom sides  
One pair of equal angles

## Sum of exterior angles

Exterior angles all add up to  $360^\circ$

Using exterior angles



$$\text{Interior angle} + \text{Exterior angle} = \text{straight line} = 180^\circ$$

$$\text{Exterior angle} = 180 - 165 = 15^\circ$$

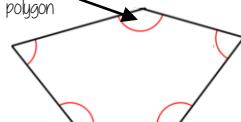
$$\text{Number of sides} = 360^\circ \div \text{exterior angle}$$

$$\text{Number of sides} = 360 \div 15 = 24 \text{ sides}$$

## Sum of interior angles

### Interior Angles

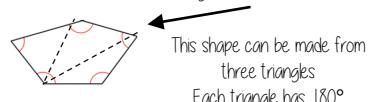
The angles enclosed by the polygon



This is an **irregular** polygon  
– the sides and angles are different sizes

$$(\text{number of sides} - 2) \times 180$$

$$\text{Sum of the interior angles} = (5 - 2) \times 180$$



$$\text{Sum of the interior angles} = 3 \times 180 = 540^\circ$$

Remember this is **all** of the interior angles added together

## Missing angles in regular polygons



$$\text{Exterior angle} = 360 \div 8 = 45^\circ$$

$$\text{Interior angle} = \frac{(8-2) \times 180}{8} = \frac{6 \times 180}{8} = 135^\circ$$

$$\text{Exterior angles in regular polygons} = 360^\circ \div \text{number of sides}$$

$$\text{Interior angles in regular polygons} = \frac{(\text{number of sides} - 2) \times 180}{\text{number of sides}}$$